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# Applications of Emad Falih Transform For General Solution of Telegraph equation 

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#### Abstract

Recently, integral transform is an important and useful tool for solving variety of problems in differential equations. Many researchers are now engaged in developing various integral transforms. In this paper we obtain the general solution of one-dimensional hyperbolic telegraph equation of second order using Emad-Falih transform.


KEY WORDS: Telegraph equation, Emad Falih transform, Integral transforms, second order one dimensional hyperbolic equation.

## I. INTRODUCTION

One dimensional second order hyperbolic telegraph equation was obtained by using Ohm's law. This equation was solved by a recent and reliable semi analytic method. The telegraph equation had been introduced by Oliver Heaviside in 1876. Telegraph equation is linear partial differential equation which describes relationship between the transmitted voltage and current with time and distance. This equation describes the reflection of the electromagnetic waves in the transmission medium. Many researchers solved this equation by using various integral transforms. Till now many researchers have developed several integral transforms Laplace, Kamal, Sadik, Elzaki, Aboodh, Mohand, Rishi, Tarig, Mahgoub EmadSara, Emad-Falih, Kushare, Soham, transforms. Integral transforms are very much useful to solve many advanced problems of science and engineering such as Radioactive decay problems, Heat conduction problems, problems of motion of the particle under gravity, Vibration of beam, problems in electric circuits, etc. Integral transforms are best tool to solve the ordinary, partial as well as fractional differential equations.

Recently, S.R Kushare and D. P. Patil [1] introduce Kushare transform in September 2021.In October 2021, S.S.Khakale and D. P. Patil [2] introduce Soham transform. As researchers are going introducing new integral transforms at the same time many researchers are interested to apply these transforms to various types of problems. In January 2022,R .S. Sanap and D. P. Patil [3] used Kushare transform to solve the problems based on Newton's law of cooling. In April 2022 D. P. Patil etc. [4] use Kushare transform to solve the problems on growth and decay. In October 2021 D. P. Patil [5] used Sawi transform in Bessel function. D. P. Patil [6] used Sawi transform of error function for evaluating improper integral further, Lpalce and Shenu transforms are used in chemical science by D. P. Patil [7]. Dr. Patil [8] solved the wave equation by Sawi transform and its convolution theorem. Further Patil [9] also used Mahgoub transform for solving parabolic boundary value problems.

Dr. Patil [10] obtains solution of the wave equation by using double Laplace and double Sumudu transform. Dualities between double integral transforms are derived by D. P. Patil [11]. Laplace, Elzaki, and Mahgoub transforms are used for solving system of first order and first degree differential equations by Kushare and Patil [12].Boundary value problems of the system of ordinary differentiable equations are by using Aboodh and Mahgoub transform by D. P. Patil [13]. D. P. Patil [14] study Laplace, Sumudu, Elzaki and Mahgoub transforms comparatively and apply them in Boundary value problems. Parabolic Boundary value problems are also solved by Dinkar Patil [15]. For that he used double Mahgoub transform.

Soham transform is used to obtain the solution of system of differential equations by D. P. Patil et al [16]. D. P. Patil et al also used Soham transform for solving Volterra integral equations of first kind [17]. D. P. Patil et al [20] used Anuj transform to solve Volterra integral equations of first kind. Rathi sisters and D. P. Patil used Soham transform for system of differential equations [21]. Recently Zankar, Kandekar and D. P. Patil used general integral transform of error

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function for evaluating improper integrals[22]. Recently, Dinkar Patil, Prerana Thakare and Prajakta Patil [23] used double general integral transform for obtaining the solution of parabolic boundary value problems. In June 2022 Shweta Vispute, Gauri Jadhav and D. P. Patil [24] used Emad Sara transform for the general solution of telegraph equation. D. P. Patil et al [25] used Soham transform for solving Newton's law of cooling. Further, HY transform is used to handling exponential growt and decay problems by Areen Shaikh, Neha More , Jaweria Shaikh and Dinkar Patil [26]. D. P. Patil , et al [27] used Emad Falih transform for solving Newton's law of Cooling.

In this paper we use Emad Falih integral transform for solving telegraph equation. This paper is organized as follows. Second section is used for preliminaries. Emad- Falih transform is used to solve telegraph equations in third section. Fourth section is devoted for conclusion.

## II. PRELIMINARIES

In this section we state some preliminary concepts which are required for solving telegraph equation by using EmadFalih transform. This section contains definition of telegraph equation, Emad Falih transform, Emad Falih transform of some fundamental functions, Emad Falih transform of derivative of functions.

## A. The Telegraph Equation: [18]

The general form of Telegraph Equation is:

$$
\frac{\partial^{2} u}{\partial t^{2}}+(\alpha+\beta) \frac{\partial u}{\partial t}+\alpha \beta u=c^{2} \frac{\partial^{2} u}{\partial x^{2}} .
$$

Where $u(x, t)$ can be voltage or current through the wire at position $x$ and time $t, \alpha=\frac{G}{C}, \beta=\frac{R}{L}$ and $c^{2}=\frac{1}{L C}$, where G is conductance of resistor, R is resistance of resistor, L is inductance of coil, and C is capacitance of capacitor.

## B. Emad - Falih Integral Transform:[19]

The Emad - Falihintegral transform is defined for an exponential order function in the set B as:

$$
\mathrm{B}=\left\{\mathrm{f}(\mathrm{t}): \mathrm{BK}, \mathrm{~m} 1, \mathrm{~m} 2>0,|\mathrm{f}(\mathrm{t})|<\mathrm{K} e^{m^{2} \mathrm{j}|t|} \text { if } \mathrm{t} \in(-1)^{\mathrm{j}} \mathrm{X}[0, \infty)\right\}
$$

Where: $f(t)$ is a function in the B set, $K$ is a finite constant number, $m 1$ and $m 2$ may or may not be finite. The kernel function of Emad-Falih integral transform symbolized by (EF) is defined by the integral equation:

$$
\mathrm{EF}\{\mathrm{f}(\mathrm{t})\}=\mathrm{T}(\phi)=\frac{1}{\varphi} \int_{0}^{\infty} e^{-\varphi^{2} t} \mathrm{f}(\mathrm{t}) \mathrm{dt}
$$

Where $\mathrm{t} \geq 0, \mathrm{~m}_{1} \leq \phi \leq \mathrm{m}_{2}$ and $\phi$ is a variable that is used as a factor to the variable t in the function f .
C. Emad-Falih integral transform for some fundamental functions:[19]

| Sr. No. | Function | Emad-Fallih <br> Transform |
| :---: | :---: | :---: |
| 1 | k | $\frac{k}{\varphi^{2}}$ |$|$| $\frac{n!}{\varphi^{2 \mathrm{n}+3}}$ |
| :---: |
| 2 |
| 3 |
| 4 |
| $\mathrm{t}^{\mathrm{n}}$ |
| 5 |

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## D. Emad-Falih Transform of derivative functions:[19]

Let $\mathrm{T}(\phi)$ is the Emad-Falilh integral transform of $[\mathrm{EF}(\mathrm{f}(\mathrm{t})=\mathrm{T}(\phi))]$, then "Emad-Falih transform" is

$$
E F\left[f^{\prime}(\mathrm{t})\right]=\frac{-f(0)}{\varphi}+\phi^{2} \mathrm{~T}(\phi)
$$

E. Emad-Falih Transform of Partial Derivative functions:[19]

Let $T(x, \alpha)$ be the Emad - Falih transform where $E F\{f(x, t)\}=T(x, \emptyset)$, then:

- $\mathrm{EF}\left[\frac{\partial f}{\partial t}\right]=\emptyset^{2} \mathrm{~T}(\mathrm{x}, \varnothing)-\frac{f(x, 0)}{\emptyset}$

Proof: $\operatorname{EF}\left(\frac{\partial f}{\partial t}\right)=\frac{1}{\emptyset} \int_{0}^{\infty} e^{-\phi^{2}} \frac{\partial F}{\partial t} \mathrm{dt}$

$$
\begin{aligned}
& =\frac{1}{\emptyset}\left\{\left[e^{-\emptyset^{2} t} \mathrm{f}(\mathrm{t})\right]_{0}^{\infty}-\int_{0}^{\infty} e^{-\emptyset^{2} t}(-\emptyset)^{2}(-\mathrm{f}(\mathrm{t}))\right\} \mathrm{dt} \\
& =\frac{1}{\varnothing}\left\{\left[(0-\mathrm{f}(0)]+\frac{1}{\emptyset} \emptyset^{2} \int_{0}^{\infty} e^{-\emptyset^{2} t} \mathrm{f}(\mathrm{t})\right\} \mathrm{dt}\right. \\
& =\left[\frac{-f(0)}{\emptyset}\right]+\emptyset^{2} \frac{1}{\emptyset} \int_{0}^{\infty} e^{-\emptyset^{2} t} \mathrm{f}(\mathrm{t}) \mathrm{dt}=\frac{-f(0)}{\emptyset}+\emptyset^{2} \mathrm{EF}[\mathrm{f}(\mathrm{t})]
\end{aligned}
$$

Thus $\operatorname{EF}\left(\frac{\partial f}{\partial t}\right)=\frac{-f(0)}{\emptyset}+\emptyset^{2} \mathrm{~T}(\emptyset)$

- $\mathrm{EF}\left[\frac{\partial^{2} \mathrm{f}}{\partial t^{2}}\right]=\emptyset^{4} \mathrm{~T}(\mathrm{x}, \varnothing)-\frac{1}{\emptyset} \frac{\partial f(x, 0)}{\partial t}-\emptyset \mathrm{f}(\mathrm{x}, 0)$

Proof: $\operatorname{EF}\left(\frac{\partial f}{\partial t}\right)=\frac{1}{\phi} \int_{0}^{\infty} e^{-\emptyset^{2} t} \frac{\partial f}{\partial t} \mathrm{dt}=\frac{1}{\phi}\left[\frac{\partial t}{\partial t} \frac{e^{-\phi^{2}} t}{-\emptyset^{2}}\right]_{0}^{\infty}-\left[\int_{0}^{\infty} \frac{\partial^{2} f}{\partial t^{2}} \frac{e^{-\phi^{2} t}}{-\emptyset^{2}} d t\right]$.

$$
\begin{gathered}
=\frac{1}{\phi}\left\{\left[\frac{\partial f(x, 0)}{\partial t} \frac{1}{\phi^{2}}\right]+\left[\frac{1}{\phi^{2}} \int_{0}^{\infty} \frac{\partial^{2} f}{\partial t^{2}} e^{-\phi^{2} t} \mathrm{dt}\right]\right\}=\frac{1}{\phi^{3}} \partial \mathrm{f}(\mathrm{x}, 0)+\frac{1}{\phi^{2}} \mathrm{EF}\left[\frac{\partial^{2} f}{\partial t^{2}}\right] \\
\therefore \frac{1}{\phi^{2}} \mathrm{EF}\left[\frac{\partial^{2} f}{\partial t^{2}}\right]=\mathrm{EF}\left[\frac{\partial f}{\partial t}\right]-\frac{1}{\phi^{3}} \frac{\partial f(x, 0)}{\partial t}
\end{gathered}
$$

Substituting $\quad \mathrm{EF}\left[\frac{\partial f}{\partial t}\right]=\emptyset^{2} T(x, \emptyset)-\frac{f(x, 0)}{\varnothing}$
$\mathrm{EF}\left[\frac{\partial^{2} f}{\partial t^{2}}\right]=\varnothing^{2}\left[\emptyset^{2} \mathrm{~T}(\mathrm{x}, \varnothing)-\frac{f(x, 0)}{\varnothing}\right]-\frac{1}{\varnothing} \frac{\partial f(x, 0)}{\partial t}$
$\mathrm{EF}\left[\frac{\partial^{2} f}{\partial t^{2}}\right]=\emptyset^{4} \mathrm{~T}(\mathrm{x}, \varnothing)-\frac{1}{\emptyset} \frac{\partial f(x, 0)}{\partial t}-\emptyset \mathrm{f}(\mathrm{x}, 0)$

## III. SOLVING TELEGRAPH EQUATIONS USING EMADFALIH TRANSFORM

In this section we solve telegraph equations by using Emad-Falih transform.
Example-1: Consider the linear equation $\frac{\partial^{2} u}{\partial x^{2}}=\frac{\partial^{2} u}{\partial t^{2}}+2 \frac{\partial u}{\partial t}+\mathrm{u}$, with initial conditions: $\mathrm{u}(\mathrm{x}, 0)=\mathrm{e}^{\mathrm{x}}$, and $\mathrm{u}_{\mathrm{t}}(\mathrm{x}, 0)=-2 \mathrm{e}^{\mathrm{x}}$
Solution: To apply Emad-Falih transform to both sides of the given equation,
$E F\left(u_{x x}\right)=E F\left(u_{t t}\right)+E F\left(u_{t}\right)+E F[u(x, t)]$
$\mathrm{T}^{\prime} \prime(\mathrm{x}, \varnothing)-\left[\varnothing^{4} \mathrm{~T}(\mathrm{x}, \varnothing)-\frac{1}{\emptyset} \frac{\partial u}{\partial t(x, 0)}-\emptyset u(x, 0)\right]-2\left[\varnothing^{2} \mathrm{~T}(\mathrm{x}, \varnothing)-\frac{u(x, 0)}{\varnothing}\right]-T(x, \emptyset)=0$
$\therefore \mathrm{T}^{\prime}(\mathrm{x}, \varnothing)-\emptyset^{4} \mathrm{~T}(\mathrm{x}, \varnothing)+\emptyset e^{\mathrm{x}}-2 \emptyset^{2} \mathrm{~T}(\mathrm{x}, \varnothing)-T(x, \emptyset)$
$\therefore \mathrm{T}^{\prime} \prime(\mathrm{x}, \varnothing)+\left(-\emptyset^{4}-2 \emptyset^{2}-1\right) \mathrm{T}(\mathrm{x}, \varnothing)=-\emptyset e^{\mathrm{x}}$
$\therefore \mathrm{T} '(\mathrm{x}, \varnothing)-\left(\varnothing^{4}+2 \emptyset^{2}+1\right) \mathrm{T}(\mathrm{x}, \varnothing)=-\varnothing e^{\mathrm{x}}$
$\therefore \frac{1}{\left(\varnothing^{4}+2 \varnothing^{2}+1\right)} \mathrm{T}^{\prime} \prime(\mathrm{x}, \varnothing)-T(x, \emptyset)=\frac{-\emptyset e^{x}}{\left(\emptyset^{4}+2 \varnothing^{2}+1\right)}$
$\therefore \frac{1}{\left(\varnothing^{2}+1\right)^{2}} \mathrm{~T}^{\prime}(\mathrm{x}, \varnothing)-\mathrm{T}(\mathrm{x}, \varnothing)=\frac{-\varnothing \text { ex }}{\left(\varnothing^{2}+1\right)^{2}}$
$\therefore \frac{D^{2} \mathrm{~T}(\mathrm{x}, \varnothing)}{\left(\varnothing^{2}+1\right)} \mathrm{T}(\mathrm{x}, \varnothing)=\frac{-\varnothing e \mathrm{x}}{\left(\varnothing^{2}+1\right)^{2}}$
$\therefore \mathrm{T}(\mathrm{x}, \varnothing)\left[\mathrm{D}^{2}-\left(\emptyset^{2}+1\right)^{2}\right]=-\varnothing \mathrm{e}^{\mathrm{x}}$
$\therefore \mathrm{T}(\mathrm{x}, \varnothing)=\frac{-\varnothing e x}{D^{2}-\left(\varnothing^{2}+1\right)^{2}} \because e^{\mathrm{x}}=\mathrm{e}^{1 \mathrm{x}}$
$\therefore \mathrm{T}(\mathrm{x}, \varnothing)=\frac{-\varnothing e x}{1-\left(\varnothing^{2}+1\right) 2}$

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$\therefore \mathrm{T}(\mathrm{x}, \emptyset)=\frac{-\emptyset e x}{1-\left(\emptyset^{4}+2 \emptyset^{2}+1\right)}$
$\therefore \mathrm{T}(\mathrm{x}, \varnothing)=\frac{-\emptyset e^{x}}{-\left(\varnothing^{4}+2 \emptyset^{2}\right)}$
$\therefore \mathrm{T}(\mathrm{x}, \varnothing)=\frac{e^{x}}{\emptyset^{3}+2 \emptyset}$
Now applying inverse Emad- Falih transform we get

$\therefore \mathrm{u}(\mathrm{x}, \mathrm{t})=\mathrm{e}^{\mathrm{x}} . \mathrm{e}^{-2 \mathrm{t}}$
$\therefore \mathrm{u}(\mathrm{x}, \mathrm{t})=\mathrm{e}^{\mathrm{x}-2 \mathrm{t}}$
Example-2: Consider the linear telegraph equation $\frac{\partial^{2} u}{\partial x^{2}}=\frac{\partial^{2} u}{\partial t^{2}}+4 \frac{\partial u}{\partial t}+4 \mathrm{u}$ with initial conditions
$u(x, 0)=1+e^{2 x}$ and $u_{t}(x, 0)=-2$
Solution:Applying Emad-Falih transform on the given equation
$\mathrm{EF}\left(\mathrm{u}_{\mathrm{xx}}\right)=\mathrm{EF}\left(\mathrm{u}_{\mathrm{tt}}\right)+\mathrm{EF}\left[4\left(\mathrm{u}_{\mathrm{t}}\right)\right]+4 \mathrm{EF}[\mathrm{u}(\mathrm{x}, \mathrm{t})]$
$\therefore \mathrm{T}^{\prime} \prime(\mathrm{x}, \varnothing)=\emptyset^{4} \mathrm{~T}(\mathrm{x}, \varnothing)-\frac{1}{\emptyset} \frac{\partial u(x, 0)}{\partial t}-\emptyset \mathrm{u}(\mathrm{x}, 0)+4 \emptyset^{2} \mathrm{~T}(\mathrm{x}, \emptyset)-\frac{4 u(x, 0)}{\emptyset}+4 \mathrm{~T}(\mathrm{x}, \varnothing)$
$\therefore \mathrm{T} '(\mathrm{x}, \varnothing)=\left(\varnothing^{4}+4 \emptyset^{2}+4\right) \mathrm{T}(\mathrm{x}, \varnothing)-\frac{2}{\emptyset}-\emptyset+\emptyset \mathrm{e}^{\mathrm{x}}-\frac{4 e^{x}}{\varnothing}$
$\therefore \mathrm{T}^{\prime \prime}(\mathrm{x}, \emptyset)-\left(\emptyset^{2}+2\right)^{2} \mathrm{~T}(\mathrm{x}, \varnothing)=-\frac{2}{\emptyset}-\emptyset+\emptyset \mathrm{e}^{\mathrm{x}}-\frac{4 e^{x}}{\varnothing}$
$\therefore \mathrm{T}(\mathrm{x}, \emptyset)\left[\mathrm{D}^{2}-\left(\emptyset^{2}+2\right)^{2}\right]=\frac{\left(-2-4 e^{x}\right)}{\emptyset}-\emptyset+\emptyset \mathrm{e}^{\mathrm{x}}$
$\therefore \mathrm{T}(\mathrm{x}, \emptyset)=\frac{\left[\frac{\left(-2-4 e^{x}\right)}{\varnothing}-\emptyset+\emptyset e^{x}\right]}{\left[\mathrm{D}^{2}-\left(\emptyset^{2}+2\right)^{2}\right]}$
Now on applying inverse Emad-Falih transform we get,
$\therefore \mathrm{EF}^{-1}[\mathrm{~T}(\mathrm{x}, \varnothing)]=\frac{\left[\frac{\left(-2-4 e^{x}\right)}{\emptyset}-\emptyset+\emptyset e^{x}\right]}{\left[\mathrm{D}^{2}-\left(\emptyset^{2}+2\right)^{2}\right]} \because \mathrm{EF}^{-1}=\left\{\frac{1}{\emptyset^{2}(\varnothing+2)}\right\}=\mathrm{e}^{-2 \mathrm{t}}$ and $\mathrm{EF}^{-1}\left\{\frac{1}{\emptyset^{3}}\right\}=1$
$\therefore \mathrm{u}(\mathrm{x}, \mathrm{t})=\mathrm{e}^{2 \mathrm{x}}+\mathrm{e}^{-2 \mathrm{t}}$

## IV. CONCLUSION

Thus Emad-Falih transform is successfully used to obtain the solution of Telegraph equation easily. The solution is correct as compared to the solution obtained by using different types of integral transforms.

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